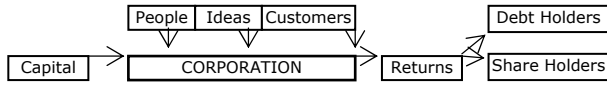


## Finance Course Review

### Introduction

**Selecting Investments:** return for risk, evaluate risk, value investment, allocation of scarce capital, tax consequences

**Financing Decisions:** source doesn't matter, incentive consequences, signals to investors, governance structure, risk mgmt



**Capital Structure:** Debt/Equity Split. Bankruptcy transfers control.

Absolute priority to debt holders after failure

**Debt and equity** -> Ownership separated from control -> Manager's job to maximize shareholder wealth

Time value of money, discount factor, present value, yield curve (usually assumed to be flat)

Capital Markets: Trade debt/equity claims; Discount factors est.; Transfer wealth in time; Transfer exp. profits future -> today

Continuous Compounding:

$$DF = e^{-Rt} \quad DF = \frac{1}{(1 + \frac{r}{freq})^{yrs \cdot freq}}$$

Perpetuity:

$$PV = \frac{C}{r}$$

Growing Perpetuity:

$$PV = \frac{C}{r-g}$$

Annuity:

$$PV = C \left( \frac{1}{r} - \frac{1}{r(1+r)^t} \right)$$

Share valuation: NPV exp. future div., i.e. growing perpetuity:  $P = \frac{DIV_1}{r-g}$   $r$  is  $CoC_E$ .  $r = \frac{DIV_1}{P_0} + g$  (div yield + div growth rate)

$g$  = plowback ratio x ROE ROE = EPS / Book Equity/Share

Plowback ratio = 1 - payout ratio = 1 - DIV/EPS

Growth stock (PVGO sig.) vs. income stock. No plowback or growth:  $r = \frac{DIV_1}{P_0} = \frac{EPS_1}{P_0}$  or  $P_0 = \frac{EPS_1}{r}$  general:  $P_0 = \frac{EPS_0}{r} + PVGO$

### Valuing Safe Projects

NPV: Depreciation (tax), allocated overhead (not included in tax), wages (full time/other project), inflation

**Working capital:** Difference between short-term assets and liabilities. Cost at beginning, same amount retrieved at end

Choosing between investments: Divide by annuity factor for equivalent annual income; assumes long lifespan, no tech/price  $\Delta$

Alternatives: **Payback pd:** ignores afterwards, some not discounted; **IRR:** project value 0, many/none poss., hard to compare

**Weak-form efficient markets:** price changes random; impossible to make consistent profits based on price histories

**Semi-strong form efficient markets:** prices reflect new information quickly; can't make much money from publicly available data

**Strong form efficient markets:** even privileged information does not give an edge, allowing for costs to gather it

### Capital Asset Pricing Model

**Cost of Capital:** return making investors indifferent to invest or not; at appropriate discount rate. NPV>0 means return>CoC

Expected return is probability weighted average return. Variance/std dev good measures of risk. Measure Volatility: Time period?

**Mean-Variance Preferences:** Exceptions (ethics, liquidity, distribution, non-standard asset).

Assumption for practical finance. Indifference curves -> rank investments, slope -> risk appetite (Joe and Camilla)

Portfolio Variance (Matrix, 2 stocks) =  $x_1^2 \sigma_1^2 + x_2^2 \sigma_2^2 + 2x_1 x_2 \rho_{12} \sigma_1 \sigma_2$  Diversification effect from negative correlation -> reduced risk

Share Beta: Sensitivity of share price to portfolio price; proportion of portfolio risk contributed by the share

$$\beta_i = \frac{\sigma_{im}}{\sigma_m} = \frac{\rho_{im} \sigma_i}{\sigma_m} \quad \text{For two stocks (weighted beta): } \beta_1 = \frac{x_1^2 \sigma_1^2 + x_1 x_2 \rho_{12} \sigma_1 \sigma_2}{\text{Portfolio Variance}}$$

If all held same portfolio, would be market portfolio; beta would be risk contribution of a share (efficient portfolio->CAPM).

Portfolio risk in mean-variance space: bows out, depending on  $\rho$ . Short stock w/ lower return to buy one w/ higher return, risk increases.

Increase number of stocks -> Efficient Set (highest possible return for a given risk), Minimum Variance Portfolio (MVP).

All hold portfolio on efficient frontier. Combos of efficient portfolios efficient -> market portfolio efficient (CAPM prediction).

Include risk free asset: Portfolios on straight line because no diversification benefit; tangential line upward dominates = Capital Market

Line, all positioned here; point on efficient set=M=Market Portfolio, 2 fund gap between  $r_f$  and M depends on risk appetite

Asset risk components (market/systemic and specific/diversifiable risk):  $\sigma^2(r) = \beta^2 \sigma^2(r_m) + \sigma^2(\epsilon)$

After diversification only market risk remains -> only rewarded for market risk

Security Market Line (Cost of Capital, expected return):  $E\{R\} = r_f + \beta(E\{r_m\} - r_f)$

Two components: Risk free rate for bearing no risk, Risk premium for bearing market risk. **Portfolio  $\beta$  = weighted avg stock  $\beta$ s**

### Valuing Risky Projects

**Company CoC** is avg of market valuations of all company projects (value of firm), provides focal point for pricing, comparison

Measuring Equity  $\beta$ /Cost of Equity: Regression, market return vs. equity return;  $R^2$  is percentage market risk.

CI for individual stock  $\beta$ s is wide. Groups of stocks -> better estimate of  $\beta$ .  $\beta$  is not stable over time.

Company Cost of Capital ignoring tax:  $r_{firm} \equiv r_{assets} = \frac{D}{V} r_{debt} + \frac{E}{V} r_{equity}$  D, E, and V are market values

Debt level increases -> debt CoC, equity CoC increase. But: D/E ratio no effect on company CoC ( $r_{firm}$ ).

$$\beta_{firm} \equiv \beta_{assets} = \frac{D}{V} \beta_{debt} + \frac{E}{V} \beta_{equity}$$

Debt level increases ->  $\beta_{debt}$  and  $\beta_{equity}$  increase,  $\beta_{firm}$  unchanged. Financial risk (nature of cash flow

claim) increases, asset risk (from nature of assets generating cash flows) unaffected.

$WACC = r_{debt} (1 - T_c) \frac{D}{V} + r_{equity} \frac{E}{V}$ ,  $T_c$ : marginal corporate tax rate (WACC after tax)

$\beta$  Estimation: Avoid errors (adjust cash flow, not DF), cyclicity (1<sup>st</sup> class): high, catastrophe insurance: low, op. leverage (high FC): high

Certainty Equivalents: Reduce the cash flows to get equivalents to discount at  $r_f$ :  $CE = \frac{Risky}{1 + \beta(\bar{r}_m - r_f)/(1 + r_f)}$

### Implementation

**Sensitivity Analysis:** Helps examine estimate quality (key variables, effects of poor estimates). Prob: Subjective estimates,

Breakeven Sales: Lowest sales to make project viable. Accountancy figures -> reduced breakeven (CoC, depreciation)

Real options (abandon, expand, wait, switch) -> Decision trees. Always increase NPV. Prob: Mkt risk changes, adjust disc. factor

Sources of economic rent: monopoly, market inefficiency, specific skills/knowledge, location, patents, brand

Principal Agent Problems: effort, perks, empire building, risk aversion: monitor through cap structure, perf-based compensation

Accounts Based Comp.: Pros: based on performance -> junior managers, Cons: manipulable, biased measures, SHolder wealth?

EVA: earnings of shareholders after CoC; Pros: CoC visible, applicable to whole business, Cons: not NPV, measures income

### Option Valuation

**Option contract** = right to perform transaction on given date **Price factors:** Time to expiry, current share price to exercise price, Volatility

Call vs. put options. American vs. European options. Premium (cost of option)

**Call Spread:** Call1-Call2 (Call2 has higher exercise price) **Straddle:** Call+Put, lose if nothing happens **Put-Call Parity:** Call-Put = Future

Option Pricing (Binomial): buy  $\Delta$  shares, B risk free bonds Option Price =  $\Delta(\text{Share Price}) + B/(1+r_f)$   $\Delta = \frac{C_u - C_d}{S_u - S_d}$   $B = \frac{C_u d - C_d u}{u - d}$

General Valuation Formula:  $C = \frac{qC_u + (1-q)C_d}{1+rt}$   $q = \frac{1+r\Delta t - d}{u-d}$  Risk neutral prob. of up mvmt  $u = e^{\sigma\sqrt{\Delta t}}$   $d = u^{-1}$   $\sigma$ : annualized volatility

Value options: Compute % up/down, Compute risk neutral probability  $q$ , Value option as if risk neutral and  $q$  is probability of up

movement, Calculate stock prices after n periods, Determine option values, Use  $q$  to work backwards to determine option price.

$\Delta$  changes every time the share price moves -> hedging required, but self-financing (no extra money in)

Black Scholes Model: infinitesimal  $\Delta t$  (continuous prices moves and hedging):

$$c = SN(d_1) - Xe^{-rt} N(d_2), \Delta = N(d_1), B = XN(d_2) \quad d_1 = \frac{\ln(S/X) + (r + \sigma^2/2)t}{\sigma\sqrt{t}} \quad \text{and} \quad d_2 = d_1 - \sigma\sqrt{t}$$

Problems w/ Black Scholes: Need ability to hedge; need to hedge continuously -> need liquid share markets, not volatile